PAPER

Mechanical quantum sensing in the search for dark matter

View the article online for updates and enhancements.

Quantum Science and Technology

Mechanical quantum sensing in the search for dark matter

D Carney[1,2,*] , G Krnjaic[2,3,*] , D C Moore[4,*] , C A Regal[5,6,*], G Afek[4], S Bhave[7],
B Brubaker[5,6], T Corbitt[8], J Cripe[9] , N Crisosto[10], A Geraci[11] , S Ghosh[1],
J G E Harris[4], A Hook[12], E W Kolb[3], J Kunjummen[1], R F Lang[13], T Li[7,13], T Lin[14], Z Liu[12],
J Lykken[2], L Magrini[15], J Manley[16], N Matsumoto[17,18,19], A Monte[2], F Monteiro[4],
T Purdy[20], C J Riedel[21], R Singh[9], S Singh[16], K Sinha[22], J M Taylor[1], J Qin[13] ,
D J Wilson[23] and Y Zhao[24]

[1] Joint Center for Quantum Information and Computer Science/Joint Quantum Institute, University of Maryland/NIST, College
     Park/Gaithersburg, MD, United States of America
[2] Fermi National Accelerator Laboratory, Batavia, IL 60510, United States of America
[3] Kavli Institute for Cosmological Physics and Enrico Fermi Institute, University of Chicago, Chicago, IL 60637, United States of
     America
[4] Wright Laboratory, Department of Physics, Yale University, New Haven, CT, United States of America
[5] JILA, National Institute of Standards and Technology/University of Colorado, Boulder, CO 80309, United States of America
[6] Department of Physics, University of Colorado, Boulder, CO 80309, United States of America
[7] Department of Electrical and Computer Engineering, Purdue University, West Lafayette, IN 47907, United States of America
[8] Department of Physics and Astronomy, Louisiana State University, Baton Rouge, LA 70803, United States of America
[9] National Institute of Standards and Technology, Gaithersburg, MD 20899, United States of America
[10] Department of Physics, University of Washington, Seattle, WA 98195, United States of America
[11] Department of Physics and Astronomy, Northwestern University, Evanston, Illinois 60208, United States of America
[12] Maryland Center for Fundamental Physics, Department of Physics, University of Maryland, College Park, MD 20742, United States of
     America
[13] Department of Physics and Astronomy, Purdue University, West Lafayette, IN 47907, United States of America
[14] Department of Physics, University of California, San Diego, CA 92093, United States of America
[15] Vienna Center for Quantum Science and Technology, Faculty of Physics, University of Vienna, A-1090 Vienna, Austria
[16] Department of Electrical and Computer Engineering, University of Delaware, Newark, DE 19716, United States of America
[17] Research Institute of Electrical Communication, Tohoku University, Sendai 980-8577, Japan
[18] Frontier Research Institute for Interdisciplinary Sciences, Tohoku University, Sendai 980-8578, Japan
[19] JST, PRESTO, Kawaguchi, Saitama 332-0012, Japan
[20] Pittsburgh Quantum Institute, University of Pittsburgh, Pittsburgh, PA 15260, United States of America
[21] NTT Research Inc., Physics & Informatics Laboratories, Sunnyvale, CA, United States of America
[22] Department of Electrical Engineering, Princeton University, Princeton, NJ 08544, United States of America
[23] Wyant College of Optical Sciences, University of Arizona, Tucson, AZ 85721, United States of America
[24] Department of Physics and Astronomy, University of Utah, Salt Lake City, UT 84112, United States of America
* Author to whom any correspondence should be addressed.

E-mail: carney@umd.edu, krnjaicg@fnal.gov, david.c.moore@yale.edu and regal@colorado.edu

Abstract

Numerous astrophysical and cosmological observations are best explained by the existence of dark matter, a mass density which interacts only very weakly with visible, baryonic matter. Searching for the extremely weak signals produced by this dark matter strongly motivate the development of new, ultra-sensitive detector technologies. Paradigmatic advances in the control and readout of massive mechanical systems, in both the classical and quantum regimes, have enabled unprecedented levels of sensitivity. In this white paper, we outline recent ideas in the potential use of a range of solid-state mechanical sensing technologies to aid in the search for dark matter in a number of energy scales and with a variety of coupling mechanisms.

1. Introduction

A significant and growing body of astrophysical [1–3] and cosmological [4, 5] observations strongly suggests the existence of 'dark matter', a massive substance which interacts very weakly—perhaps only

through gravity—with ordinary, visible matter. This dark matter has not yet been observed at particle colliders or in dedicated searches [6]. Many dark matter direct detection experiments to date have focused on weakly interacting massive particles (WIMPs) with masses around 100 GeV. These technologies are reaching full maturity, and will have either detected or largely excluded WIMPs as viable dark matter candidates within the next generation of experiments [7]. There is thus a clear need for searches of new dark matter candidates, with new experimental techniques [8].

Precision measurement techniques harnessing ideas developed in the atomic, optical, and quantum sensing fields have increasingly been deployed in the search for dark matter (see e.g. [9, 10] for reviews). In this white paper, we discuss approaches to searching for dark matter using massive, mechanical sensing devices. We include applications of purely classical mechanical sensors, as well as many devices which are now operating in the 'quantum-limited' regime, in which the dominant noise contributions come from the quantum mechanics of measurement itself. These ultra-high precision systems can enable tests of a wide range of dark matter models with extremely small couplings to ordinary matter (both electromagnetic and otherwise). These approaches complement existing search strategies, and in many cases provide better sensitivity than other available options.

The development of mechanical detectors has a rich history. Precision measurement in the context of gravitational physics has utilized a range of large-scale systems such as optical interferometers [11], atom interferometers [12, 13], torsion balances [14, 15], and Weber bars [16, 17]. Beyond application to gravitational waves, classical and quantum detectors based on mechanical elements have been constructed at widely disparate mass scales-ranging from single ions [18, 19], to tens of thousands of atoms [20], to microscale resonators [21, 22] and up to kilogram-scale devices [11, 14]. In this white paper, we consider how a variety of mechanical systems can open fundamentally new avenues to search for dark matter over a large range of energy scales. In particular, monitoring solid, massive objects allows for coherent integration of long-wavelength interactions, and for integration of small cross sections over large volumes or large numbers of target atoms or nuclei. Mechanical devices that are read out interferometrically at the shot-noise limit, or even at or below the standard quantum limit (SQL) enforced by quantum backaction [23], have been demonstrated across a wide range of mass scales, with natural frequencies ranging from millihertz to gigahertz in recent years (see [24] for a review). Hence, multiple technologies are at an opportune point for contemplating their role in precision experiments.
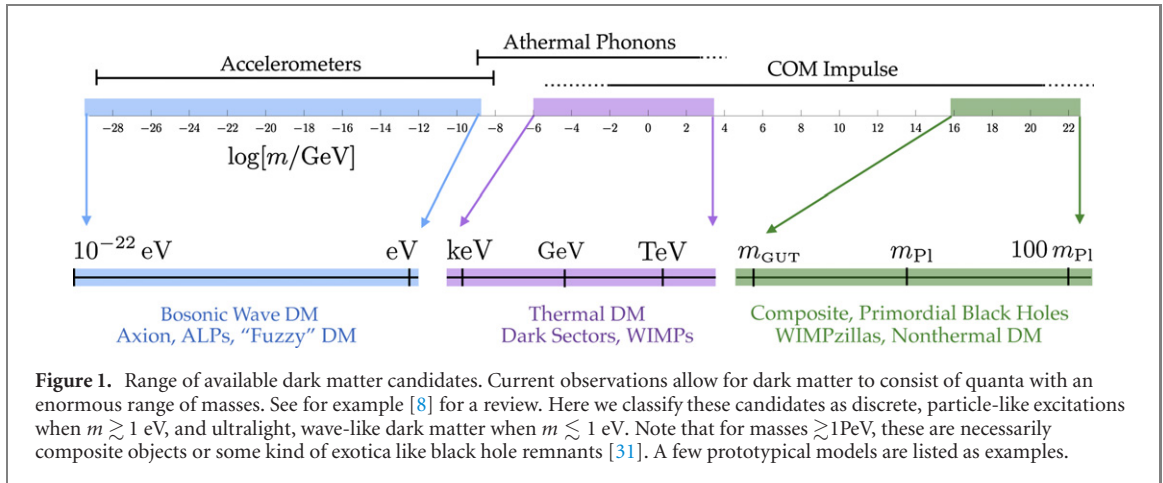
Dark matter detection is a particularly compelling and challenging problem, which may require the development of fundamentally new technologies. Mechanical detection may be poised to contribute to these challenging searches in both near-term and long-term experiments. Development of new technologies will necessarily proceed with researchers in the sensing and particle physics communities working in tandem. In the following, we outline opportunities and objectives in this new direction in the search for dark matter. We note that the mechanical sensing techniques we focus on have many similarities to proposed dark matter searches with atom interferometry [25–27] and atomic clock systems [28–30].

2. Motivations for mechanical sensors

The present landscape of viable dark matter candidates is enormous, leading to a wide variety of potential experimental signatures. Dark matter candidates could range in mass from 10^{-22} eV up to hundreds of solar masses, a range of some 90 orders of magnitude.[25] See figure 1 for a non-exhaustive breakdown of this range. Moreover, dark matter could interact with the standard model through many possible interactions, although perhaps only through gravity. To span this diverse range of possible models, different regions of parameter space will require different detector architectures and measurement techniques. In particular, for models interacting with the standard model only through mass or other extensive quantities such as nucleon number, massive mechanical sensors may be required. Mechanical sensing technologies offer an extensive set of platforms, as discussed in section 4, and thus have the potential to search for a wide range of such dark matter candidates in regions of parameter space that are complementary to existing searches.

The ability to monitor a large number of atoms in aggregate offers two key advantages over other approaches. The first advantage is the large volume integration of any putative dark matter signal. Any dark–visible interactions are necessarily tiny, so using a large volume (or a large mass of target nuclei or atoms, for models that can resolve the underlying substructure of the masses) is key to meaningful detection prospects. The second advantage is that long-wavelength signals can be integrated coherently across the full device, leading to greatly enhanced sensitivities. Such coherent detection has applications in the search for signals from wave-like dark matter signals like the axion or other ultralight bosons, as well as

---

[25] In this paper, we use natural units $\hbar = c = 1$ to quote particle physics quantities like masses and momenta.

Figure 1. Range of available dark matter candidates. Current observations allow for dark matter to consist of quanta with an enormous range of masses. See for example [8] for a review. Here we classify these candidates as discrete, particle-like excitations when $m \gtrsim 1$ eV, and ultralight, wave-like dark matter when $m \lesssim 1$ eV. Note that for masses $\gtrsim 1$PeV, these are necessarily composite objects or some kind of exotica like black hole remnants [31]. A few prototypical models are listed as examples.

in the case of impulses delivered with extremely small momentum transfers. In section 3, we give some examples of dark matter models leading to these types of signals, and discuss prospects for their detection with mechanical sensors.

3. Detection targets and techniques

Possible signals of dark matter are controlled by a few key parameters. Astrophysical observations tell us that the dark matter mass density in our neighborhood is $\rho \sim 0.3$ GeV cm^{-3} [32]. Assuming this dark matter consists of a single component, with (unknown) mass of an individual dark matter quantum, m_χ, this means that the local number density is around
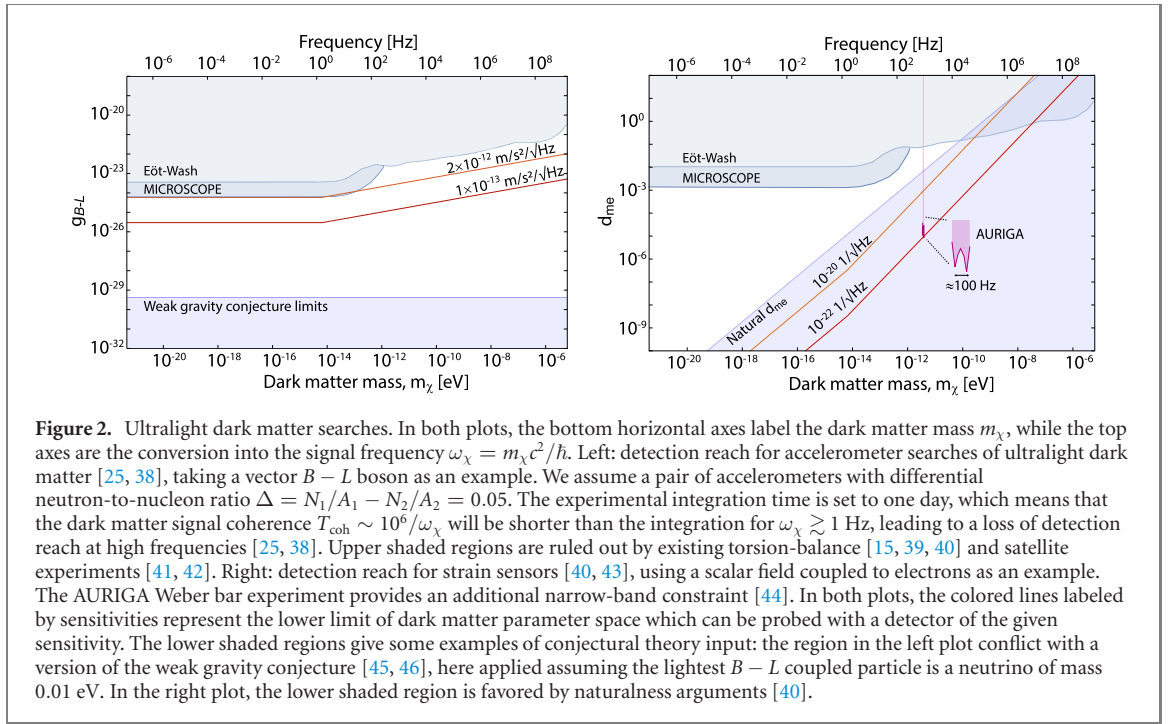
$$n_\chi = \frac{0.3}{\text{cm}^{-3}} \times \left(\frac{1 \text{ GeV}}{m_\chi} \right). \tag{1}$$

Moreover, the Earth is moving through the virialized background dark matter with 'wind speed' $v_{\text{DM}} \sim 200$ km s^{-1}, typically assumed to follow a Maxwellian velocity distribution cutoff by the galactic escape velocity of $\sim$550 km s^{-1} [33, 34]. These parameters fix the kinematics of any detection experiment. The only additional information is what non-gravitational couplings, if any, the dark matter has with visible matter. See e.g. [35] for a review and further references.

Broadly speaking, the above properties mean that potential dark matter signals fall into two classes determined by the dark matter particle mass (see figure 1). Traditional DM detection has focused on dark matter candidates of masses greater than around $m_\chi \gtrsim 1$ eV, which appear as distinct particles. If these interact with visible matter, they will deposit tiny, discrete impulses (on the order of $p = m_\chi v_{\text{DM}}$) when they collide with a detector. On the other hand, ultralight dark matter fields of mass 10^{-22} eV $\lesssim m_\chi \lesssim 1$ eV have enormous occupation numbers, given equation (1). The low mass means that the field must be bosonic, since otherwise Pauli exclusion would not allow enough quanta into the galactic halo. This combined with the high occupation number of the quanta mean that the field behaves as a background of oscillating waves of wavelength $\lambda_{\text{dB}} \gtrsim 1$ mm. This background of waves will be coherent over a timescale $T_{\text{coh}} \sim 10^6 / \omega_\chi$ set by Doppler broadening, where $\omega_\chi = m_\chi c^2 / \hbar$ is the natural frequency of the field [36, 37]. These models thus produce extremely weak, coherent, persistent signals. Searching for these two classes of signals requires different measurement techniques, which we now discuss separately in more detail.

3.1. Ultralight searches

Consider a scenario where a sizeable fraction of the dark matter mass density is made up of a single ultralight field. Examples of such ultralight dark matter candidates include the axion [36], vector bosons arising by gauging the conservation of baryon minus lepton number $(B - L)$ [25] or dark photons [47], scalar and pseudoscalar fields coupled through the Higgs portal [48] or the stress tensor [29] (see table 1 of reference [25] for a collation of allowed couplings). These models are minimal in the sense that they add only a single field to the standard model of particle physics, and introduce no ultraviolet anomalies. The axion couples directly to the electromagnetic and gluon fields, and can thus be searched for using a variety of systems including microwave cavities [49, 50] and NMR systems [51, 52]. The other candidates, however, can couple to quantities proportional to mass density. It is thus natural to search for these types of DM with massive sensors.

Figure 2. Ultralight dark matter searches. In both plots, the bottom horizontal axes label the dark matter mass m_χ, while the top axes are the conversion into the signal frequency $\omega_\chi = m_\chi c^2/\hbar$. Left: detection reach for accelerometer searches of ultralight dark matter [25, 38], taking a vector $B - L$ boson as an example. We assume a pair of accelerometers with differential neutron-to-nucleon ratio $\Delta = N_1/A_1 - N_2/A_2 = 0.05$. The experimental integration time is set to one day, which means that the dark matter signal coherence $T_{\rm coh} \sim 10^6/\omega_\chi$ will be shorter than the integration for $\omega_\chi \gtrsim 1$ Hz, leading to a loss of detection reach at high frequencies [25, 38]. Upper shaded regions are ruled out by existing torsion-balance [15, 39, 40] and satellite experiments [41, 42]. Right: detection reach for strain sensors [40, 43], using a scalar field coupled to electrons as an example. The AURIGA Weber bar experiment provides an additional narrow-band constraint [44]. In both plots, the colored lines labeled by sensitivities represent the lower limit of dark matter parameter space which can be probed with a detector of the given sensitivity. The lower shaded regions give some examples of conjectural theory input: the region in the left plot conflict with a version of the weak gravity conjecture [45, 46], here applied assuming the lightest $B - L$ coupled particle is a neutrino of mass 0.01 eV. In the right plot, the lower shaded region is favored by naturalness arguments [40].

If DM consists primarily of one of these ultralight fields, the observable signature is an oscillating background of ultralight bosons. This produces a nearly monochromatic, sinusoidal force signal in a massive detector, with strength proportional to the mass, leading to a variety of physical effects. For scalar DM the variations of fundamental constants such as the electron mass, or fine structure constant would lead to a periodic strain in macroscopic devices, and the possibility of detecting it has been explored in several mechanical structures [40, 43, 44, 53, 54]. For pseudoscalar DM candidates, observable signatures can include time-varying nucleon electric dipole moments, spin-torques, and EMFs along magnetic fields [25]. For vector DM one can obtain material dependent couplings, leading to differential accelerations. For a concrete example, consider a vector boson field A_μ arising from a gauged $B - L$ symmetry. This couples to the neutron field n through the neutron number density, that is, through a coupling $g_{B-L}A\bar{n}n$. The dark matter background of vector bosons then leads to a force on a sensor given by

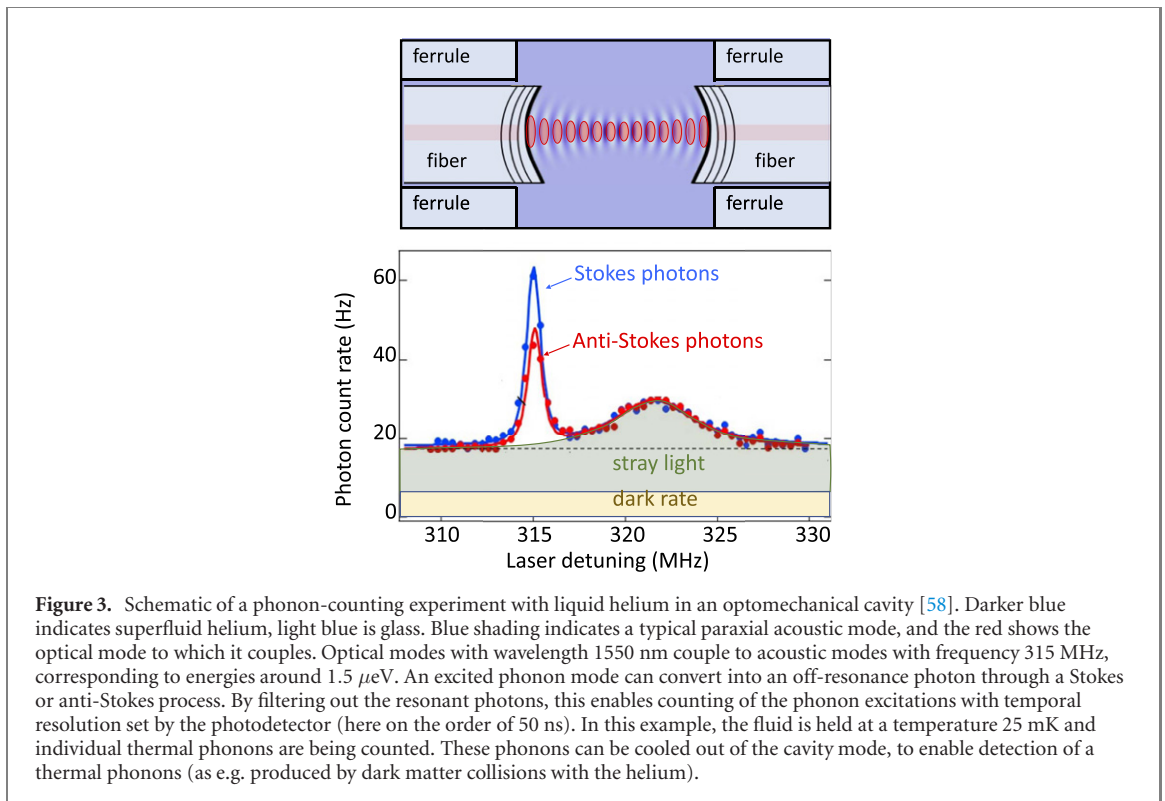$$F(t) = F_0 N_{\rm n} g_{B-L} \cos(\omega_\chi t) \tag{2}$$

where $N_{\rm n}$ is the number of neutrons in the sensor, $F_0 = \sqrt{\rho_{\rm DM}} \sim 10^{-15}$ N is set by the dark matter density (1), and g_{B-L} is an unknown but weak coupling strength [25, 38]. Since the coupling is to neutron number as opposed to total mass, a pair of sensors with different neutron-to-nucleon ratios N/A can be used to search for the differential acceleration produced by (2). In figure 2, we plot the available parameter space in this scenario and the acceleration sensitivities needed for novel searches.

At the core, the detection problem here is to sense a weak, persistent, narrow-band signal. Coherent sensing of narrowband forces is a prototypical application of mechanical sensors, and so these are ideal detection targets for which mechanical sensors are poised to make an immediate impact, particularly at higher frequencies (Hz–GHz) and/or using multiple sensors to coherently integrate the signal.

3.2. Particle-like searches based on recoils

Dark matter candidates of mass $m_\chi \gtrsim 1$ eV, on the other hand, will behave like discrete particles, calling for a different set of detection techniques. To highlight the core challenges in this regime, we can consider the case of traditional WIMP searches [55].[26] In a liquid noble detector, the WIMPs would occasionally strike an atomic nucleus, causing it to recoil. If sufficient energy was deposited, the nucleus ionizes or excites nearby atoms, leading to either electron–ion pairs or emission of scintillation photons which can then be detected by charge sensors or photodetectors at the edges of the detector. This example demonstrates the basic issues: the events are very rare (owing to the tiny dark matter-nucleon cross sections, $\sigma \lesssim 10^{-36}$ cm^2 [56]) and the energy deposition is very small (a given WIMP has mass of about $\sim$100 protons and velocity

---

[26] Note that the term 'WIMP' traditionally refers to $m_\chi \gtrsim 1$ GeV fermions. Additional complications can arise, for example for lighter candidates $m_\chi \lesssim 100$ MeV, where coherent and inelastic scattering effects can become important. However, these concerns do not change the basic picture of the DM signal as small, rare recoil events.

Figure 3. Schematic of a phonon-counting experiment with liquid helium in an optomechanical cavity [58]. Darker blue indicates superfluid helium, light blue is glass. Blue shading indicates a typical paraxial acoustic mode, and the red shows the optical mode to which it couples. Optical modes with wavelength 1550 nm couple to acoustic modes with frequency 315 MHz, corresponding to energies around 1.5 μeV. An excited phonon mode can convert into an off-resonance photon through a Stokes or anti-Stokes process. By filtering out the resonant photons, this enables counting of the phonon excitations with temporal resolution set by the photodetector (here on the order of 50 ns). In this example, the fluid is held at a temperature 25 mK and individual thermal phonons are being counted. These phonons can be cooled out of the cavity mode, to enable detection of a thermal phonons (as e.g. produced by dark matter collisions with the helium).

10^5 m s^{-1}) leading to only small amounts of ionization or scintillation. Thus any detection program needs to have sufficient target mass to see enough events, as well as very low detection thresholds to see these small energy deposits. We note that many other signals of interest, in particular low-energy neutrinos [57], have precisely the same properties.

The massive mechanical sensing paradigm offers a straightforward solution to the issue of mass: for example, the LIGO detectors have mechanical elements (the interferometer mirrors) with masses of tens of kilograms! On the other hand, smaller mechanical detectors can also enable extremely low-threshold energy detection. There are two basic strategies: detection of localized phonons in bulk materials, and direct monitoring of impulses to the center of mass motion of a single device.

A number of proposals for the detection of dark matter through bulk phononic excitations currently exist [59–63], which may extend the sensitivity beyond existing implementations of phonon sensing in cryogenic calorimeters (e.g. [64–66]). For example, when a dark matter particle interacts with a nucleus in a bulk crystal, it generates a distortion of the lattice, exciting phonons. The phonons then travel through the material, and can be sensed by calorimetric detectors at the edges of the material. As an example, state-of-the-art transition edge sensors can resolve a total deposited energy in phonons down to energies around few $\times$ 10 meV [67]. This means that searches of this type are sensitive to 'light' dark matter candidates, of masses in the eV–MeV range. Optomechanical readout of phonons in small samples can reach substantially lower thresholds. For example, single phonons at the micro-eV level can be read out in micromechanical oscillators [68, 69] superfluid helium [58] or bulk crystals [70]; we show the superfluid helium example in figure 3. The primary challenge in such systems is not energy threshold, but instead coupling energy into the phonon modes of interest (which are often purposefully decoupled from the bulk phonon modes in the system to avoid thermal noise). In addition, such systems are small (with mode masses at the μg to mg scale), so scaling up to a sufficient volume for non-trivial dark matter detection reach is an interesting open problem. If coupling of phonons into the modes of interest could be engineered (even with relatively low efficiencies) such techniques would provide an exciting complement to calorimetric phonon detection experiments.

Alternatively, one can monitor the center of mass motion of an entire object (i.e. the zero-mode phonon). This technique could be particularly advantageous in the setting where the collision acts coherently on the entire mechanical component, for example when the dark matter couples to the sensor through a long-range force. Here one continuously monitors the center of mass position and looks for small transfers of momenta greater than the typical noise on the device. The noise floor is ultimately limited by thermal coupling with the environment and by quantum mechanical measurement noise coming from the monitoring of the device [23, 76]. Concretely, the SQL provides a benchmark for a detectable impulse [77,
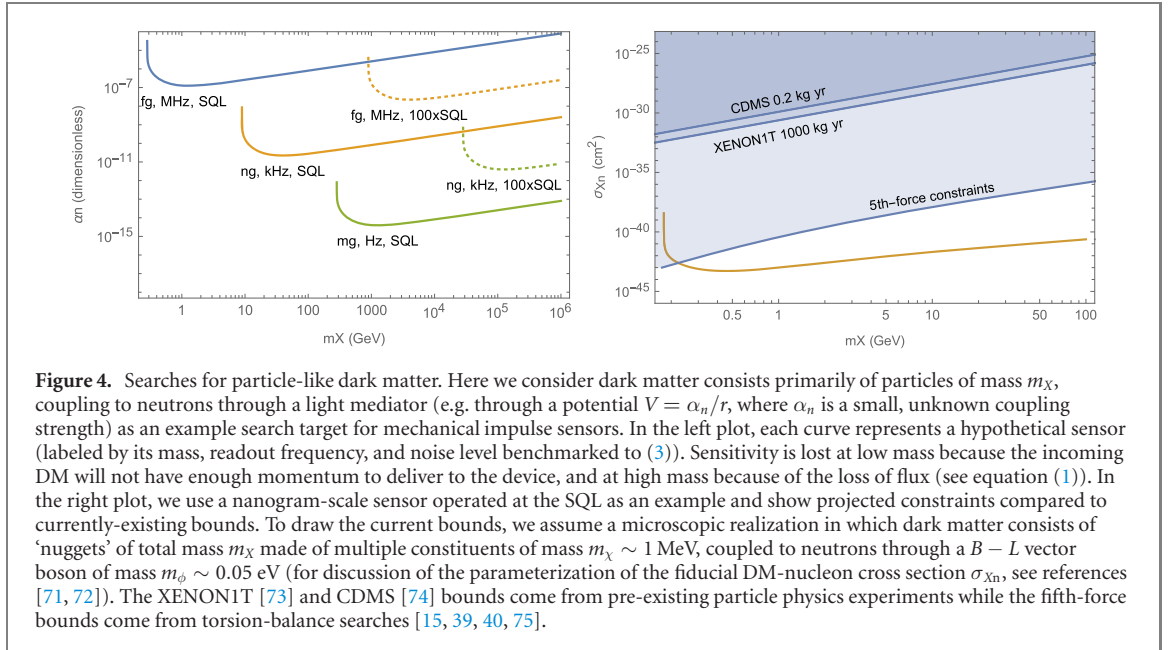
Figure 4. Searches for particle-like dark matter. Here we consider dark matter consists primarily of particles of mass m_X, coupling to neutrons through a light mediator (e.g. through a potential $V = \alpha_n/r$, where α_n is a small, unknown coupling strength) as an example search target for mechanical impulse sensors. In the left plot, each curve represents a hypothetical sensor (labeled by its mass, readout frequency, and noise level benchmarked to (3)). Sensitivity is lost at low mass because the incoming DM will not have enough momentum to deliver to the device, and at high mass because of the loss of flux (see equation (1)). In the right plot, we use a nanogram-scale sensor operated at the SQL as an example and show projected constraints compared to currently-existing bounds. To draw the current bounds, we assume a microscopic realization in which dark matter consists of 'nuggets' of total mass m_X made of multiple constituents of mass $m_\chi \sim 1\,\mathrm{MeV}$, coupled to neutrons through a $B - L$ vector boson of mass $m_\phi \sim 0.05\,\mathrm{eV}$ (for discussion of the parameterization of the fiducial DM-nucleon cross section σ_{Xn}, see references [71, 72]). The XENON1T [73] and CDMS [74] bounds come from pre-existing particle physics experiments while the fifth-force bounds come from torsion-balance searches [15, 39, 40, 75].

78]:

$$\Delta p_{SQL} = \sqrt{\hbar m \omega} \approx 1.5\,\mathrm{MeV} \times \left(\frac{m}{1\,\mathrm{ng}} \right)^{1/2} \left(\frac{\omega/2\pi}{1\,\mathrm{kHz}} \right)^{1/2}, \tag{3}$$

where m, ω are the mass and frequency of the mechanical sensor.[27] The SQL is the best signal to noise possible as enforced by a balance of imprecision and quantum backaction for a typical interferometer, and for a resonant detector corresponds to resolving at the level of mechanical vacuum fluctuations [23]. While methods exist to go below this noise level (see section 4), currently existing devices acting at or even slightly above the SQL are already capable of searching novel regions of DM parameter space, as demonstrated by the initial search in [72]. For example, a dark matter particle with mass m_χ could transfer a maximum momentum to a mechanical sensor of $\Delta p = 2m_\chi v$ where $v \sim 10^{-3}c$. For sufficiently large couplings that a substantial fraction of the dark matter momentum is transferred to the mechanical sensor, this permits detection of impulses from dark matter particles as light as $\gtrsim 1\,\mathrm{GeV}$ for a ng mass at the SQL as in equation (3). We describe an example in figure 4.

3.3. Direct gravitational interaction with heavy dark matter

As an ultimate long-term goal, mechanical sensing could open the possibility of direct detection of heavy ($m_\chi \gtrsim m_{Planck} \sim 0.02\,\mathrm{mg}$) dark matter *purely through its gravitational interaction with visible matter* [79–81]. This coupling is the only one guaranteed to exist, so an experiment with sufficient sensitivity would have the ability to find or completely rule out any dark matter candidate in the mass range for which it is sensitive. This proposal involves the direct monitoring of impulses delivered to sizeable (gram-scale) mechanical sensors, and exploits the coherent nature of the gravitational interaction. Achieving this goal would require realizing noise levels well below the SQL impulse sensing limit, as well as the ability to build and read out a large array of sensors. However, the concept employed is precisely the same as that described in the previous section, namely observation of an impulse to the center of mass of an object. The basic idea can thus be tested in prototype experiments, for example [72].

4. Available mechanical sensors and future challenges

Mechanical devices have been demonstrated with masses from single ions to kilograms, and on frequency scales from millihertz to gigahertz. Precision sensing has long used massive detectors in the context of gravitational wave searches employing interferometric or resonant detectors, e.g. LIGO. On a smaller scale, accelerometers and other mechanical devices are ubiquitous in modern technology, and increasingly specialized mechanical systems with extreme environmental isolation are important tools for storage and transduction of quantum information [24].

---

[27] Here, the frequency ω should be replaced by the inverse measurement times scale when this exceeds the mechanical frequency, such as the free-mass case $\omega \to 0$.

Table 1. Examples of currently-available mechanical sensors. Sensitivities for continuous sensing are represented by the relevant noise power spectral densities (e.g. S_a is the acceleration noise power), or threshold (σ_E is the single-phonon detection threshold). Here we summarize solid-state mechanical detectors, although atom interferometers can be characterized by similar metrics. We include single ions as a comparative point.

Physical device	Mass	Frequency	Temp.	Quantum limit	Sensitivity, e.g. acceleration, strain, force
Resonant acoustic wave:					
BAW/Weber bar [44]	1000 kg	1 kHz	4 K		$h_s \sim 10^{-21}$ Hz$^{-1/2}$
HBAR/phonon counting [82]	50 μg	10 GHz	10 mK	single phonon	$\sigma_E \sim 30\ \mu$eV $h_s \sim 10^{-15}$ Hz$^{-1/2}$ ($h_s \sim 10^{-9}$ Hz$^{-1/2}$ below res)
superfluid helium cavities [58]	1 ng	300 MHz	50 mK	single phonon	$\sigma_E \sim 1\ \mu$eV
Resonant and below-resonance detectors:					
Cantilever optomechanical accelerometer [83]	25 mg	10 kHz	300 K		$\sqrt{S_a} \sim 3 \times 10^{-9}$ g Hz$^{-1/2}$ ($\sqrt{S_a} \sim 10^{-7}$ g Hz$^{-1/2}$ below res)
SiN-suspended test mass accelerometer [84, 85]	10 mg	10 kHz	300 K		$\sqrt{S_a} \sim 10^{-7}$ g Hz$^{-1/2}$ ($\sqrt{S_a} \sim 10^{-6}$ g Hz$^{-1/2}$ below res)
SiN membrane optomechanics [86–92]	10 ng	1.5 MHz	100 mK	at SQL	$\sqrt{S_a} \sim 10^{-7}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 10^{-17}$ N Hz$^{-1/2}$
Crystalline cantilever for force sensing [93]	0.2 ng	1 kHz	200 mK		$\sqrt{S_a} \sim 3 \times 10^{-7}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 10^{-18}$ N Hz$^{-1/2}$
Pendula above resonance:					
LIGO mirror [94]	10 kg	10 Hz–10 kHz	300 K	Shot noise limited above 100 Hz	$\sqrt{S_a} \sim 4 \times 10^{-15}$ g Hz$^{-1/2}$ at 100 Hz $\sqrt{S_x} \sim 10^{-19}$ m Hz$^{-1/2}$
Suspended mg mirror [95–97]	1 mg	1–10 kHz	300 K	Factor of 20 in displacement from SQL	$\sqrt{S_a} \sim 7 \times 10^{-11}$ g Hz$^{-1/2}$ at 600 Hz $\sqrt{S_x} \sim 5 \times 10^{-17}$ m Hz$^{-1/2}$
Crystalline cantilever [98]	50 ng	10–100 kHz	300 K	at SQL	$\sqrt{S_a} \sim 2 \times 10^{-7}$ g Hz$^{-1/2}$ at 20 kHz $\sqrt{S_x} \sim 10^{-16}$ m Hz$^{-1/2}$
Levitated and free-fall systems:					
LISA pathfinder [99]	15 kg	1–30 mHz	300 K		$\sqrt{S_a} \sim 10^{-15}$ g Hz$^{-1/2}$
Magnetically-levitated mm-scale sphere [100]	4 mg	20 Hz	5 K		$\sqrt{S_a} \sim 2 \times 10^{-7}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 8 \times 10^{-12}$ N/$\sqrt{\text{Hz}}$
Magnetically-levitated sub-mm sphere [101]	0.25 μg	1–20 Hz	Feedback cool to 9 K		$\sqrt{S_a} \sim 10^{-7}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 2 \times 10^{-16}$ N/$\sqrt{\text{Hz}}$
Optically trapped microsphere [102]	1 ng	10–100 Hz	Feedback cool to 50 μK	Factor of 100 in displacement from SQL	$\sqrt{S_a} \sim 10^{-7}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 10^{-18}$ N Hz$^{-1/2}$
Optically trapped nanosphere [103, 104] (rotational [105])	3 fg	300 kHz	Laser cool to 12 μK	Ground state	$\sqrt{S_a} \sim 7 \times 10^{-4}$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 2 \times 10^{-20}$ N Hz$^{-1/2}$ $\sqrt{S_\tau} \sim 10^{-27}$ Nm Hz$^{-1/2}$
Trapped ion crystal [18] (for comparison)	10^{-6} fg	1 MHz			$\sqrt{S_a} \sim 50$ g Hz$^{-1/2}$ $\sqrt{S_f} \sim 4 \times 10^{-22}$ N Hz$^{-1/2}$

As discussed above, many of the scientific motivations favor larger volumes or masses to increase the rate of dark matter interactions in the detector. This motivates use of more massive systems, which also provide better sensitivity to accelerations (scaling as the square root of the mass). However, also important are the energy range of interest, the available probes of specific mechanical modes, ever-present noise sources, and scalability. To understand the scope of different available platforms, we present in table 1 different detector types, and a sampling of sensitivities achieved to date in specific experiments. This list is meant to be exemplary, and not exhaustive, and part of the challenge of advancing dark matter detection with mechanical sensors is matching technologies with the different dark matter candidates and couplings we outlined in section 3. The parameters in the table can also be considered a starting point, i.e. rapid progress in mechanical detectors is being made in many fields, and as exemplified in the workshop on which this white paper is based, there is increasing cross-development between sensors of widely differing scales that will lead to fruitful technical improvements.

Here we briefly exemplify the opportunities associated with the different physical architectures presented in table 1. For cases where an impulse detector is desired, an essentially free mass can be created by using a low-frequency pendulum measured above its resonance frequency, i.e. at time-scales faster than an oscillation period. An interesting alternative is to levitate particles and then release them after state preparation to perform measurements in free-fall. Ultralight searches are likely to be first pursued by resonant detectors—ideally tunable resonant detectors. The center of mass motion of a cantilever, membrane [106], or even levitated sphere are appropriate in this situation. For ultralight searches that result in changes in atomic strain due to effective signatures that appear as time-variations in fundamental constants or atomic length scales, and hence excitation of effective breathing modes, bulk acoustic modes are of interest [43]. Importantly, detection of such bulk acoustic waves may scale to large volumes using clever readout techniques, as exemplified by recent single-phonon detection of a bulk acoustic resonator [82], and in the long-standing ability to read out motion of very large Weber bars [16, 17]. Athermal phonon detection may also benefit from this scaling if athermal phonons created in the bulk of a material could be coupled into the readout modes of interest, but could also be pursued in arrays of smaller sensors. Different devices can also support detection of additional signatures or couplings, e.g. electric or magnetic charges or the material polarizability.

The quest to go beyond the sensitivities presented in table 1 is ongoing, and we list here a few examples of how advances in both conventional and non-conventional technologies for precision sensors are poised to make interesting progress. Superfluid helium is a pristine system that hosts mechanical modes; recent advances [58] in observing the quantum motion of this liquid in a small cavity are promising, and this system could be easily scalable to larger volumes and number of samples by simply immersing more probes in a single vat of liquid helium. SiN micromechanical membranes offer a unique possibility to use strain to move the resonant frequency of a mechanical detector by orders of magnitude while maintaining low dissipation [107], allowing searches over a wide range of DM masses. By expanding to larger membranes [106, 108] it should be possible to achieve kHz-scale resonant detectors with much larger masses than traditional cantilevers. While optical readout is typical of precision interferometry, electrical readout is poised to make important contributions, both in the context of phonon readout through superconducting qubits [82], but also through advances in magnetic couplings [109]. Detection of the motion of levitated nanospheres is reaching quantum measurement limits [103]. Scaling the mass of levitated systems in the quantum regime to the ng scale and above may offer extremely low threshold mechanical sensors with substantial mass that are well-isolated from environmental noise [100, 102, 110]. Readout of ultra low-energy phonons is currently achieved in small devices; if these techniques could be adapted to read out larger volumes—and if the challenging problem of coupling energy from such a volume into the modes of interest could be overcome—the potential gains are significant. Lastly, the growth of gravitational wave astronomy will undoubtedly bring advances in materials for mirrors, mirror coatings, and suspensions that will advance all precision measurements based upon suspended pendula.

Reducing both technical and quantum measurement-added noise sources will allow for progressively increasing sensitivity to dark matter. In general, devices operating at lower frequencies tend to be dominated by thermal or other technical noise sources, while higher-frequency devices are limited by shot noise or more generally by quantum measurement noise. The ubiquitous problem of thermal noise can be mitigated by isolating a mechanical sensing device from its environment. This environmental decoupling is often characterized via the quality factor Q of the resonator, which is given by the ratio of the resonant mechanical frequency to the dissipation rate, $Q = \omega_\mathrm{m}/\gamma_\mathrm{m}$. The heating rate of a sensor can be expressed as $k_\mathrm{b}T_\mathrm{bath}/Q$. The source of environmental dissipation in mechanical devices is a deep subject studied in many contexts. Dissipation can be traced to lossy materials; for example, material damping associated with mirror coatings is an important contributor to noise in LIGO [111]. Dissipation can also be traced to radiation of acoustic energy out of the mechanical mode of interest; for example, phononic bandgap engineering has become a fruitful path to reducing radiation loss in high-frequency mechanical devices. The continued development of lower dissipation (higher-Q) devices will be of critical importance to the sensitivity of mechanical dark matter detection.

We can see directly in table 1 that a range of experiments are now impinging on quantum noise limits, and so methods to operate devices well into the quantum-limited regime (i.e. true 'quantum sensors') are of substantial interest. Measurement-added noise has been suppressed below the shot noise limit at LIGO [112], and it has likewise been driven to the SQL [86, 98] and beyond [87] with membranes and cantilevers. Quantum sensing techniques can further reduce these noise levels using squeezed readout light [113, 114] and/or a variety of backaction-evasion techniques [115–118]. In the context of free-mass targets, femtogram levitated spheres have been cooled to their quantum ground state [103]. Ultimately, to detect momentum transfers far below the SQL, it may be necessary to prepare the mechanics in a more extreme non-classical state, such as a coherent spatial superposition, and then perform interferometric measurement

[119–121]. The sensitivity of such superpositions to small impulses is in principle unbounded, scaling with the spatial extent and temporal duration of the quantum coherence that is achieved. In addition to sub-SQL sensitivities to classical forces, such an approach can offer the unique possibility of detecting sources of anomalous test-mass diffusion (e.g., DM-induced Brownian motion), which can cause decoherence in a matter interferometer [122, 123] even when the mean momentum transfer is negligible [124].

Construction and operation of an *array of mechanical sensors* poses an interesting technical challenge with applications to many of the dark matter searches described above. Performing differential measurements on multiple sensors would allow for rejection of many backgrounds. In particular, use of sensors with different materials will enable discrimination against signals which act in a material-independent fashion, for example gravitational noise. Relative accelerations between objects with different numbers of neutrons could identify ultralight fields coupling to $B - L$. Coherent integration of multiple sensors would be highly valuable, enabling scaling in sensitivity that is linear with the number N of sensors as opposed to the incoherent $\sqrt{N}$ enhancement. Understanding the detailed nature of sensor–sensor interactions in a tightly packed array will be important. These interactions could be exploited to enhance measurement sensitivity, in particular through entanglement of multiple sensors [125].

In the near term, a number of demonstrator experiments could pave the way for future, scalable dark matter detection. Given the current constraints on ultralight dark matter, current or near future devices could already perform non-trivial searches in this parameter space. Operating a small array of sensors as a coherent detector of ultralight dark matter would demonstrate the basic techniques needed as well as help to identify challenges in scaling to larger numbers. Moving toward detection of short impulses, demonstration of ultra-low threshold phonon readout in a meaningful volume would be of substantial value. Demonstrating that optomechanical impulse sensing allows for backaction noise evasion would likewise be extremely valuable, and allow for a more detailed understanding of the potential limitations of such a technique, in particular due to optical losses.

5. Conclusions

Dark matter constitutes one of the most fundamental mysteries in modern science: what is the nature of this strange mass, taking up a quarter of the Universe's energy budget? As the search for dark matter enters maturity, new theoretical and experimental directions are needed. Mechanical sensing technologies, especially with quantum-sensing techniques that can enable measurement past traditional quantum limits, offer an exciting route to new experimental searches.

Deploying currently available technology could have immediate impact, while longer-term prospects will require some technical advances. On the experimental side, a number of basic technological challenges to be overcome and demonstrations of the core search techniques will be of critical importance. Data processing techniques and the application of lessons learned from previous experiments about the nature of potential background signals will require development tailored to these experimental approaches. Looking toward the longer term, interdisciplinary collaborative efforts and the construction and use of multiple sensors as a coherent detector offer a fascinating set of problems.

Overall, the wide variety of platforms and scales available with these techniques has the potential to make significant impact across a wide swath of the dark matter landscape. Future developments should only continue to improve sensitivities and detection reach. Further collaboration between the mechanical quantum sensing and particle physics communities will undoubtedly lead to even more possibilities than those outlined here.

Acknowledgments

ORCID iDs

D Carney ⓘ https://orcid.org/0000-0002-4269-8342
D C Moore ⓘ https://orcid.org/0000-0002-2358-4761
J Cripe ⓘ https://orcid.org/0000-0002-0977-8711
A Geraci ⓘ https://orcid.org/0000-0001-7009-0118
J Qin ⓘ https://orcid.org/0000-0001-8228-8949
D J Wilson ⓘ https://orcid.org/0000-0002-0822-9892

References

[1] Sofue Y and Rubin V 2001 Rotation curves of spiral galaxies *Annu. Rev. Astron. Astrophys.* **39** 137–74
[2] Markevitch M, Gonzalez A H, Clowe D, Vikhlinin A, Forman W, Jones C, Murray S, Tucker W and Tucker W 2004 Direct constraints on the dark matter self-interaction cross-section from the merging galaxy cluster 1E0657-56 *Astrophys. J.* **606** 819–24
[3] Massey R, Kitching T and Richard J 2010 The dark matter of gravitational lensing *Rep. Prog. Phys.* **73** 086901
[4] Primack J R 2015 Cosmological structure formation *The Philosophy of Cosmology* (Cambridge: Cambridge University Press) pp 136–60
[5] Aghanim N *et al* (Planck Collaboration) 2018 Planck 2018 results. VI. Cosmological parameters (arXiv:1807.06209 [astro-ph.CO])
[6] Bertone G and Hooper D 2018 History of dark matter *Rev. Mod. Phys.* **90** 045002
[7] Arcadi G, Dutra M, Ghosh P, Lindner M, Mambrini Y, Pierre M, Profumo S and Queiroz F S 2018 The waning of the wimp? A review of models, searches, and constraints *Eur. Phys. J.* C **78** 203
[8] Battaglieri M *et al* 2017 Us cosmic visions: new ideas in dark matter 2017: community report (arXiv:1707.04591)
[9] Ahmed Z *et al* 2018 Quantum Sensing for High Energy Physics *First workshop on Quantum Sensing for High Energy Physics Lemont* (IL, USA December 12–14 2017)
[10] Safronova M S, Budker D, DeMille D, Kimball D F J, Derevianko A and Clark C W 2018 Search for new physics with atoms and molecules *Rev. Mod. Phys.* **90** 025008
[11] Abramovici A *et al* 1992 LIGO: the laser interferometer gravitational-wave observatory *Science* **256** 325–33
[12] Kasevich M and Chu S 1992 Measurement of the gravitational acceleration of an atom with a light-pulse atom interferometer *Appl. Phys.* B **54** 321–32
[13] Peters A, Chung K Y and Chu S 2001 High-precision gravity measurements using atom interferometry *Metrologia* **38** 25
[14] Hoyle C D, Schmidt U, Heckel B R, Adelberger E G, Gundlach J H, Kapner D J and Swanson H E 2001 Submillimeter test of the gravitational inverse-square law: a search for large extra dimensions *Phys. Rev. Lett.* **86** 1418
[15] Wagner T A, Schlamminger S, Gundlach J H and Adelberger E G 2012 Torsion-balance tests of the weak equivalence principle *Class. Quantum Grav.* **29** 184002
[16] Weber J 1966 Observation of the thermal fluctuations of a gravitational-wave detector *Phys. Rev. Lett.* **17** 1228
[17] Cerdonio M *et al* 1997 The ultracryogenic gravitational-wave detector Auriga *Class. Quantum Grav.* **14** 1491
[18] Biercuk M J, Uys H, Britton J W, VanDevender A P and Bollinger J J 2010 Ultrasensitive detection of force and displacement using trapped ions *Nat. Nanotechnol.* **5** 646
[19] Ivanov P A, Vitanov N V and Singer K 2016 High-precision force sensing using a single trapped ion *Sci. Rep.* **6** 28078
[20] Schreppler S, Spethmann N, Brahms N, Botter T, Barrios M and Stamper-Kurn D M 2014 Optically measuring force near the standard quantum limit *Science* **344** 1486–9
[21] Teufel J D, Donner T, Castellanos-Beltran M A, Harlow J W and Lehnert K W 2009 Nanomechanical motion measured with an imprecision below that at the standard quantum limit *Nat. Nanotechnol.* **4** 820
[22] Peterson R, Purdy T, Kampel N, Andrews R, Yu P-L, Lehnert K and Regal C 2016 Laser cooling of a micromechanical membrane to the quantum backaction limit *Phys. Rev. Lett.* **116** 063601
[23] Caves C M 1980 Quantum-mechanical radiation-pressure fluctuations in an interferometer *Phys. Rev. Lett.* **45** 75
[24] Aspelmeyer M, Kippenberg T J and Marquardt F 2014 Cavity optomechanics *Rev. Mod. Phys.* **86** 1391
[25] Graham P W, Kaplan D E, Mardon J, Rajendran S and Terrano W A 2016 Dark matter direct detection with accelerometers *Phys. Rev. D* **93** 075029
[26] Geraci A A and Derevianko A 2016 Sensitivity of atom interferometry to ultralight scalar field dark matter *Phys. Rev. Lett.* **117** 261301
[27] Coleman J (MAGIS-100 Collaboration) 2019 Matter-wave atomic gradiometer interferometricSensor (MAGIS-100) at fermilab *PoS* 21
[28] Derevianko A and Pospelov M 2014 Hunting for topological dark matter with atomic clocks *Nat. Phys.* **10** 933
[29] Arvanitaki A, Huang J and Van Tilburg K 2015 Searching for dilaton dark matter with atomic clocks *Phys. Rev. D* **91** 015015
[30] Stadnik Y and Flambaum V 2015 Searching for dark matter and variation of fundamental constants with laser and maser interferometry *Phys. Rev. Lett.* **114** 161301
[31] Griest K and Kamionkowski M 1990 Unitarity limits on the mass and radius of dark–matter particles *Phys. Rev. Lett.* **64** 615–8
[32] Read J I 2014 The local dark matter density *J. Phys. G: Nucl. Part. Phys.* **41** 063101
[33] Kafle P R, Sharma S, Lewis G F and Bland-Hawthorn J 2014 On the shoulders of giants: properties of the stellar halo and the milky way mass distribution *Astrophys. J.* **794** 59
[34] Piffl T *et al* 2014 The RAVE survey: the Galactic escape speed and the mass of the milky way *Astron. Astrophys.* **562** A91
[35] Lin T 2019 Dark matter models and direct detection *PoS* **333** 009
[36] Sikivie P 1983 Experimental tests of the invisible axion *Phys. Rev. Lett.* **51** 1415
[37] Hu W, Barkana R and Gruzinov A 2000 Fuzzy cold dark matter: the wave properties of ultralight particles *Phys. Rev. Lett.* **85** 1158
[38] Carney D, Hook A, Liu Z, Taylor J M and Zhao Y Ultralight dark matter detection with mechanical quantum sensors (arXiv:1908.04797 [hep-ph])

[39] Schlamminger S, Choi K-Y, Wagner T A, Gundlach J H and Adelberger E G 2008 Test of the equivalence principle using a rotating torsion balance *Phys. Rev. Lett.* **100** 041101

[40] Arvanitaki A, Dimopoulos S and Van Tilburg K 2016 Sound of dark matter: searching for light scalars with resonant-mass detectors *Phys. Rev. Lett.* **116** 031102

[41] Hees A, Minazzoli O, Savalle E, Stadnik Y V and Wolf P 2018 Violation of the equivalence principle from light scalar dark matter *Phys. Rev.* D **98** 064051

[42] Bergé J, Brax P, Métris G, Pernot-Borràs M, Touboul P and Uzan J-P 2018 Microscope mission: first constraints on the violation of the weak equivalence principle by a light scalar dilaton *Phys. Rev. Lett.* **120** 141101

[43] Manley J, Stump R, Wilson D, Grin D and Singh S 2019 Searching for scalar dark matter with compact mechanical resonators (arXiv:1910.07574)

[44] Branca A *et al* 2017 Search for an ultralight scalar dark matter candidate with the auriga detector *Phys. Rev. Lett.* **118** 021302

[45] Arkani-Hamed N, Motl L, Nicolis A and Vafa C 2007 The string landscape, black holes and gravity as the weakest force *J. High Energy Phys.* JHEP06(2007)060

[46] Cheung C, Liu J and Remmen G N 2018 Proof of the weak gravity conjecture from black hole entropy *J. High Energy Phys.* JHEP10(2018)004

[47] Pierce A, Riles K and Zhao Y 2018 Searching for dark photon dark matter with gravitational-wave detectors *Phys. Rev. Lett.* **121** 061102

[48] Piazza F and Pospelov M 2010 Sub-ev scalar dark matter through the super-renormalizable Higgs portal *Phys. Rev.* D **82** 043533

[49] Du N *et al* 2018 Search for invisible axion dark matter with the axion dark matter experiment *Phys. Rev. Lett.* **120** 151301

[50] Zhong L *et al* 2018 Results from phase 1 of the Haystac microwave cavity axion experiment *Phys. Rev.* D **97** 092001

[51] Arvanitaki A and Geraci A A 2014 Resonantly detecting axion-mediated forces with nuclear magnetic resonance *Phys. Rev. Lett.* **113** 161801

[52] Budker D, Graham P W, Ledbetter M, Rajendran S and Sushkov A O 2014 Proposal for a cosmic axion spin precession experiment (casper) *Phys. Rev. X* **4** 021030

[53] Geraci A A, Bradley C, Gao D, Weinstein J and Derevianko A 2019 Searching for ultralight dark matter with optical cavities *Phys. Rev. Lett.* **123** 031304

[54] McNally R L and Zelevinsky T 2020 Constraining domain wall dark matter with a network of superconducting gravimeters and LIGO *Eur. Phys. J. D* **74** 1–6

[55] Schumann M 2019 Direct detection of WIMP dark matter: concepts and status *J. Phys. G: Nucl. Part. Phys.* **46** 103003

[56] Akerib D S *et al* (LUX Collaboration) 2017 Results from a search for dark matter in the complete LUX exposure *Phys. Rev. Lett.* **118** 021303

[57] Cabrera B, Krauss L M and Wilczek F 1985 Bolometric detection of neutrinos *Phys. Rev. Lett.* **55** 25

[58] Shkarin A, Kashkanova A, Brown C, Garcia S, Ott K, Reichel J and Harris J 2019 Quantum optomechanics in a liquid *Phys. Rev. Lett.* **122** 153601

[59] Guo W and McKinsey D N 2013 Concept for a dark matter detector using liquid helium-4 *Phys. Rev.* D **87** 115001

[60] Schutz K and Zurek K M 2016 Detectability of light dark matter with superfluid helium *Phys. Rev. Lett.* **117** 121302

[61] Griffin S, Knapen S, Lin T and Zurek K M 2018 Directional detection of light dark matter with polar materials *Phys. Rev.* D **98** 115034

[62] Knapen S, Lin T, Pyle M and Zurek K M 2018 Detection of light dark matter with optical phonons in polar materials *Phys. Lett.* B **785** 386–90

[63] Kurinsky N A, Yu T C, Hochberg Y and Cabrera B 2019 Diamond detectors for direct detection of sub-GeV dark matter *Phys. Rev.* D **99** 123005

[64] Agnese R *et al* (SuperCDMS Collaboration) 2017 Projected sensitivity of the supercdms SNOLAB experiment *Phys. Rev.* D **95** 082002

[65] Abdelhameed A H *et al* (CRESST Collaboration) 2019 First results from the crest-III low-mass dark matter program *Phys. Rev.* D **100** 102002

[66] Armengaud E *et al* (EDELWEISS Collaboration) 2019 Searching for low-mass dark matter particles with a massive ge bolometer operated above ground *Phys. Rev.* D **99** 082003

[67] Fink C *et al* Characterizing TES power noise for future single optical-phonon and infrared-photon detectors (arXiv:2004.10257 [physics.ins-det])

[68] Cohen J D, Meenehan S M, MacCabe G S, Gröblacher S, Safavi-Naeini A H, Marsili F, Shaw M D and Painter O 2015 Phonon counting and intensity interferometry of a nanomechanical resonator *Nature* **520** 522–5

[69] Riedinger R, Hong S, Norte R A, Slater J A, Shang J, Krause A G, Anant V, Aspelmeyer M and Gröblacher S 2016 Non-classical correlations between single photons and phonons from a mechanical oscillator *Nature* **530** 313–6

[70] Jain V, Yoon T, Lei C U, Chu Y, Frunzio L, Rakich P and Schoelkopf R 2020 Listening to bulk crystalline vibrations with superconducting qubits *Bull. Am. Phys. Soc.* **65**

[71] Coskuner A, Grabowska D M, Knapen S and Zurek K M 2019 Direct detection of bound states of asymmetric dark matter *Phys. Rev.* D **100** 035025

[72] Monteiro F, Afek G, Carney D, Krnjaic G, Wang J and Moore D C Search for composite dark matter with optically levitated sensors (arXiv:2007.12067 [hep-ex])

[73] Aprile E *et al* (XENON Collaboration) 2017 First dark matter search results from the XENON1T experiment *Phys. Rev. Lett.* **119** 181301

[74] Agnese R *et al* (SuperCDMS Collaboration) 2018 Low-mass dark matter search with CDMSlite *Phys. Rev.* D **97** 022002

[75] Heeck J 2014 Unbroken B—L symmetry *Phys. Lett.* B **739** 256–62

[76] Caves C M 1981 Quantum-mechanical noise in an interferometer *Phys. Rev.* D **23** 1693

[77] Mozyrsky D, Martin I and Hastings M 2004 Quantum-limited sensitivity of single-electron-transistor-based displacement detectors *Phys. Rev. Lett.* **92** 018303

[78] Clerk A 2004 Quantum-limited position detection and amplification: a linear response perspective *Phys. Rev.* B **70** 245306

[79] Kawasaki A 2019 Search for kilogram-scale dark matter with precision displacement sensors *Phys. Rev.* D **99** 023005

[80] Hall E D, Adhikari R X, Frolov V V, Müller H and Pospelov M 2018 Laser interferometers as dark matter detectors *Phys. Rev.* D **98** 083019

[81] Carney D, Ghosh S, Krnjaic G and Taylor J M Gravitational direct detection of dark matter (arXiv:1903.00492 [hep-ph])

[82] Chu Y, Kharel P, Renninger W H, Burkhart L D, Frunzio L, Rakich P T and Schoelkopf R J 2017 Quantum acoustics with
      superconducting qubits *Science* eaao1511
[83] Guzmán Cervantes F, Kumanchik L, Pratt J and Taylor J M 2014 High sensitivity optomechanical reference accelerometer over
      10 kHz *Appl. Phys. Lett.* **104** 221111
[84] Zhou F, Bao Y, Long D, Madugani R, Gorman J and LeBrun T 2019 Testing of an optomechanical accelerometer with a
      high-finesse on-chip microcavity *CLEO: QELS_Fundamental Science* (Optical Society of America) pp JW2A–4A
[85] Krause A G, Winger M, Blasius T D, Lin Q and Painter O 2012 A high-resolution microchip optomechanical accelerometer *Nat.
      Photon.* **6** 768
[86] Kampel N S, Peterson R W, Fischer R, Yu P-L, Cicak K, Simmonds R W, Lehnert K W and Regal C A 2017 Improving broadband
      displacement detection with quantum correlations *Phys. Rev.* X **7** 021008
[87] Mason D, Chen J, Rossi M, Tsaturyan Y and Schliesser A 2019 Continuous force and displacement measurement below the
      standard quantum limit *Nat. Phys.* **15** 745–9
[88] Underwood M, Mason D, Lee D, Xu H, Jiang L, Shkarin A B, Børkje K, Girvin S M and Harris J G E 2015 Measurement of the
      motional sidebands of a nanogram-scale oscillator in the quantum regime *Phys. Rev.* A **92** 061801
[89] Tsaturyan Y, Barg A, Polzik E S and Schliesser A 2017 Ultracoherent nanomechanical resonators via soft clamping and
      dissipation dilution *Nat. Nanotechnol.* **12** 776
[90] Norte R A, Moura J P and Gröblacher S 2016 Mechanical resonators for quantum optomechanics experiments at room
      temperature *Phys. Rev. Lett.* **116** 147202
[91] Reetz C, Fischer R, Assumpcao G G, McNally D P, Burns P S, Sankey J C and Regal C A 2019 Analysis of membrane phononic
      crystals with wide band gaps and low-mass defects *Phys. Rev. Appl.* **12** 044027
[92] St-Gelais R, Bernard S, Reinhardt C and Sankey J C 2019 Swept-frequency drumhead optomechanical resonators *ACS Photonics*
      6 525–30
[93] Mamin H J and Rugar D 2001 Sub-attonewton force detection at millikelvin temperatures *Appl. Phys. Lett.* **79** 3358–60
[94] Martynov D V *et al* 2016 Sensitivity of the advanced LIGO detectors at the beginning of gravitational wave astronomy *Phys. Rev.*
      D **93** 112004
[95] Corbitt T *et al* 2007 An all-optical trap for a gram-scale mirror *Phys. Rev. Lett.* **98** 150802
[96] Matsumoto N, Cataño-Lopez S B, Sugawara M, Suzuki S, Abe N, Komori K, Michimura Y, Aso Y and Edamatsu K 2019
      Demonstration of displacement sensing of a mg-scale pendulum for mm-and mg-scale gravity measurements *Phys. Rev. Lett.*
      122 071101
[97] Cataño-Lopez S B, Edamatsu K and Matsumoto N 2019 High *q* mg-scale monolithic pendulum for quantum-limited gravity
      measurements (arXiv:1912.12567)
[98] Cripe J *et al* 2019 Measurement of quantum back action in the audio band at room temperature *Nature* **568** 364–7
[99] Anderson G *et al* 2018 Experimental results from the ST7 mission on LISA pathfinder *Phys. Rev.* D **98** 102005
[100] Timberlake C, Gasbarri G, Vinante A, Setter A and Ulbricht H 2019 Acceleration sensing with magnetically levitated oscillators
      above a superconductor *Appl. Phys. Lett.* **115** 224101
[101] Lewandowski C W, Knowles T D, Etienne Z B and D'Urso B High sensitivity accelerometry with a feedback-cooled magnetically
      levitated microsphere (arXiv:2002.07585 [physics.app-ph])
[102] Monteiro F, Li W, Afek G, Li C-l, Mossman M and Moore D C 2020 Force and acceleration sensing with optically levitated
      nanogram masses at microkelvin temperatures *Phys. Rev.* A **101** 053835
[103] Delić U, Reisenbauer M, Dare K, Grass D, Vuletić V, Kiesel N and Aspelmeyer M 2020 Cooling of a levitated nanoparticle to the
      motional quantum ground state *Science* **367** 892–5
[104] Tebbenjohanns F, Frimmer M, Jain V, Windey D and Novotny L 2020 Motional sideband asymmetry of a nanoparticle optically
      levitated in free space *Phys. Rev. Lett.* **124** 013603
[105] Ahn J, Xu Z, Bang J, Ju P, Gao X and Li T 2020 Ultrasensitive torque detection with an optically levitated nanorotor *Nat.
      Nanotechnol.* **15** 89–93
[106] Manley J, Chowdhury M D, Grin D, Singh S and Wilson D J Searching for vector dark matter with an optomechanical
      accelerometer (arXiv:2007.04899 [quant-ph])
[107] Thompson J D, Zwickl B M, Jayich A M, Marquardt F, Girvin S M and Harris J G E 2008 Strong dispersive coupling of a
      high-finesse cavity to a micromechanical membrane *Nature* **452** 72–5
[108] Moura J P, Norte R A, Guo J, Schäfermeier C and Gröblacher S 2018 Centimeter-scale suspended photonic crystal mirrors *Opt.
      Express* **26** 1895–909
[109] Zoepfl D, Juan M, Schneider C and Kirchmair G 2019 Single-photon strong cooperativity in microwave magneto-mechanics
      (arXiv:1912.05489)
[110] Childress L, Schmidt M, Kashkanova A, Brown C, Harris G, Aiello A, Marquardt F and Harris J 2017 Cavity optomechanics in a
      levitated helium drop *Phys. Rev.* A **96** 063842
[111] Saulson P R 1990 Thermal noise in mechanical experiments *Phys. Rev.* D **42** 2437
[112] Abadie J *et al* 2011 A gravitational wave observatory operating beyond the quantum shot-noise limit *Nat. Phys.* **7** 962
[113] Aasi J *et al* 2013 Enhanced sensitivity of the LIGO gravitational wave detector by using squeezed states of light *Nat. Photon.* **7**
      613–9
[114] Tse M *et al* 2019 Quantum-enhanced advanced LIGO detectors in the era of gravitational-wave astronomy *Phys. Rev. Lett.* **123**
      231107
[115] Braginsky V B, Vorontsov Y I and Thorne K S 1980 Quantum nondemolition measurements *Science* **209** 547–57
[116] Pereira S F, Ou Z Y and Kimble H J 1994 Backaction evading measurements for quantum nondemolition detection and
      quantum optical tapping *Phys. Rev. Lett.* **72** 214
[117] Clerk A A, Marquardt F and Jacobs K 2008 Back-action evasion and squeezing of a mechanical resonator using a cavity detector
      New J. Phys. **10** 095010
[118] Ghosh S, Carney D, Shawhan P and Taylor J M Back-action evading impulse measurement with mechanical quantum sensors
      (arXiv:1910.11892 [quant-ph])
[119] Geraci A and Goldman H 2015 Sensing short range forces with a nanosphere matter-wave interferometer *Phys. Rev.* D **92**
      062002
[120] Wan C, Scala M, Morley G, Rahman A A, Ulbricht H, Bateman J, Barker P, Bose S and Kim M 2016 Free nano-object Ramsey
      interferometry for large quantum superpositions *Phys. Rev. Lett.* **117** 143003

[121] Pino H, Prat-Camps J, Sinha K, Venkatesh B P and Romero-Isart O 2018 On-chip quantum interference of a superconducting microsphere *Quantum Sci. Technol.* **3** 025001

[122] Riedel C J 2013 Direct detection of classically undetectable dark matter through quantum decoherence *Phys. Rev.* D **88** 116005

[123] Riedel C J and Yavin I 2017 Decoherence as a way to measure extremely soft collisions with dark matter *Phys. Rev.* D **96** 023007

[124] Riedel C J 2015 Decoherence from classically undetectable sources: standard quantum limit for diffusion *Phys. Rev.* A **92** 010101

[125] Giovannetti V, Lloyd S and Maccone L 2004 Quantum-enhanced measurements: beating the standard quantum limit *Science* **306** 1330–6